# MINISTRY OF EDUCATION AND SCIENCE OF UKRAINE National Aviation University

Faculty of Air Navigation, Electronics and Telecommunications Department of Aviation Computer-Integrated Complexes

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" " 2022	""2022



Quality management system

# EXTENDED PROGRAM

on

**«Optimal Control Systems»** 

Educational Professional Program: "Computer-Integrated Technological Processes and Production"

Field of study: 15 «Automation and Instrumentation»

Specialty: 151 «Automation and Computer-Integrated Technologies»

Training Form	Seme- ster	Total (hours/credits ECTS)	Lec- tures	Pract. classes	Lab. classes	Self-study	HT/ CGP/ CW	TP/CP	Semester Grade
Day Form	2	120/4,0	18	-	18	84	-	-	Graded test –2 s

Index CM - 2 - 151 - 2 / 21 - 3.4



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The Extended Program on «Optimal Control Systems» is developed on the basis of the Educational Professional Program «Computer-integrated technological processes and production», Curriculum and Extended Curriculum of Education Seekers Training for «Master» CM - 2 - 151 - 2/21 and ECM - 2 - 151 - 2/21 for the Specialty 151 "Automation and Computer-Integrated Technologies" and corresponding normative documents

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#### INTRODUCTION

The Extended Program on «Optimal Control Systems» is developed on the basis of "Methodical instructions for the development and design of the Extended Program for the subject", enacted by the order as of 29.04.2021 № 249/oд and corresponding normative documents.

#### 1. EXPLANATORY NOTE

### 1.1. Place, objectives, tasks of the subject.

**The place** of the subject «Optimal Control Systems» in the system of professional training.

The educational subject refers to the disciplines of free choice of students. The discipline is the theoretical basis of the set of knowledge and skills that form the profile of a specialist in the field of automation and computer-integrated technologies.

The aim of teaching the discipline is to create a complex of knowledge on the synthesis of optimal control systems, as well as control and operation of modern optimal control systems as part of computer-integrated complexes.

### Tasks of the discipline are:

- formation of stable knowledge on methods of synthesis of optimal management systems and methods of quality analysis of management processes and correction of dynamic properties of systems;
- formation of practical skills in designing and using optimal management systems.

### 1.2. Learning outcomes the subject makes it possible to achieve.

The study of the academic discipline involves the formation of the following program learning outcomes in the applicants:

- to design, modify and research optimal computer-integrated control systems;
- analyze the structure and algorithms of optimal management systems.

## 1.3. Competences the subject makes it possible to acquire.

As a result of studying this discipline, the student acquires the following **program competencies**:

- 3K2 the ability to generate new ideas (creativity);
- CK3 the ability to apply modeling and optimization methods to research and improve the efficiency of systems and processes of managing complex technological and organizational-technical objects in aviation;
- CK6 the ability to apply problem-oriented methods of analysis, synthesis and optimization of automation systems, cyber-physical productions, processes of managing technological complexes.

### 1.4. Interdisciplinary connections.

The educational discipline «Optimal Control Systems» is based on the knowledge of such disciplines as «Methods of Modeling and Optimization of Systems and Processes», «Applied Identification Theory» and interacts with the discipline «Algorithmic and Information Support of Computer-Integrated Systems», which are studied in parallel with it and complement each other one.



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#### 2. COURSE TRAINING PROGRAM ON THE SUBJECT.

### 2.1. The subject content

The educational material of the subject «Optimal Control Systems» is structured on a modular principle and consists of two educational modules, namely:

- educational module No. 1 "Methodological foundations of optimal control systems";
- educational **module No. 2 "Methods of dynamic optimization of control"**, each of which is logically complete, independent and integral part of the curriculum. Its mastering has in view module test and analysis of its completion.

### 2.2. Modular structuring and integrated requirements for each module

### Module No. 1 "Methodological foundations of optimal control systems"

### **Integrated requirements of module No 1:**

Knows

- algebraic criteria in management problems and static optimization.

#### Be able:

- perform synthesis of limited controls for autonomous systems.

### Topic 1. Introduction to the theory of optimal management

Introduction to the theory of optimization and optimal control. Classification of optimal control systems. Static and dynamic optimization. General formulation of the problem of optimal management. Optimality criteria. Theoretical and functional restrictions on state and control vectors.

### Topic 2. Algebraic criteria in management problems

Controllability of linear non-stationary systems. Area of reach. Controllability criterion. Controllability of linear stationary systems. Observability and identifiability of linear systems. Observers. The principle of duality of management and monitoring tasks. Problems of synthesis of limited controls for autonomous systems. Management of linear systems with incomplete measurements.

### Topic 3. Static optimization

Methods of finding the unconditional extremum of the optimality criterion. Minimum necessary and sufficient conditions. Methods of conditional optimization in the presence of autonomous constraints-inequalities and constraints of the type of connections. Multi-criteria optimization. Pareto set. Schemes of compromises.

### Module No. 2 "Methods of dynamic optimization of control"

#### **Integrated requirements of module No 2:**

Know:

- methods of dynamic optimization.

#### Be able:

- perform synthesis of optimal control algorithms.

### Topic 1. Variational methods of dynamic optimization

Necessary and sufficient conditions for the minimum functional. Conditions of transversality. Generalization of the problem of unconditional optimization for the case of many variables. Application of variational calculus methods to optimal control problems. Linear optimal control. Optimal control with a generalized quality indicator.



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### Topic 2. Pontryagin's maximum principle in optimal control problems

Hamilton's function. Optimality conditions in the Pontryagin form are necessary. Maximum control system speed. Determination of strategy and optimal control algorithm. The impact of disturbances and inaccuracies in the assignment of object parameters on the quality and stability of high-speed systems.

### Topic 3. Dynamic programming method in control tasks

Bellman's principle of optimality. Minimum error function. Bellman's functional and differential equation. Synthesis of optimal control algorithms by the method of dynamic programming.

### Topic 4. Analytical design of optimal control systems

Formulation of problems of analytical design of an optimal regulator. The Letov-Kalman method. The Letov-Kalman theorem. O. A. Krasovsky's method. O. A. Krasovsky's theorem.

### 2.3. Training schedule of the subject.

		A	Cadem	ic hour	`S
№	Торіс	Total	Lectures	Lab. classes	Self-study
	Module №1 «Methodological foundations of optim	nal coi	ntrol sy	stems»	
1.1	Introduction to the theory of entired control		2 sen	nester	
1.1	Introduction to the theory of optimal control	14	2	2	10
1.2	Algebraic criteria in control problems	20	2 2	2	14
1.3	Static optimization	16	2	2	12
1.4	Module test 1	6	-	2	4
	Total for Module 1	56	8	8	40
	Module №2 «Methods of dynamic optimiza	tion of	contro	l»	
2.1	Variational methods of dynamic optimization	14	2	2	10
2.2	Pontryagin's maximum principle in optimal control problems	16	2 2	2	10
2.3	Dynamic programming method in control tasks	14	2	2	10
2.4	Analytical design of optimal control systems	14	2	2	10
2.5	Module test 2	6	-	2	4
	Total for Module 2	64	10	10	44
	Total for the discipline	120	18	18	84



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#### 3. BASIC CONCEPTS OF GUIDANCE ON THE SUBJECT

#### 3.1. Teaching methods

Both subject-oriented and individually-oriented learning technologies are used to activate the educational and cognitive activity of students during the study of the discipline. Laboratory work mainly uses the Case Study method, and lectures and presentations and interactive learning technologies are used.

#### 3.2. List of references

#### **Basic literature**

- 3.2.1. Тунік А.А., Абрамович О.О. Основи сучасної теорії управління. Навчальний посібник. К.: Видавництво Національного авіаційного університету «НАУдрук», 2010. 260 с.
- 3.2.2. Конспект лекцій «Сучасна теорія управління, методи синтезу та оптимізації управління» / Успенський В.Б., Шипуліна Л.В. Х.: НТУ "ХПІ", 2013. 136 с.
- 3.2.3. Тютюнник А. Г. Оптимальні та адаптивні системи автоматичного керування: навчальний посібник для студ. вузів. ЖІТІ. Житомир, 2002.
- 3.2.4. Desineni Subbaram Naidu. Optimal control systems. Boca Raton, Fla. : CRC Press, 2003. 433 p.
- 3.2.5. Lawrence C. Evans. An Introduction to Mathematical Optimal Control Theory.

  Berkeley: University of California, 2010. 126 p.

#### Additional literature

- 3.2.6. Соколов С. В. Оптимальні та адаптивні системи : навчальний посібник / Суми : Сумський державний університет, 2018. –221 с.
- 3.2.7. Бабак В. П., Синєглазов В. М., Таранов С. Г. Самоналагоджувальні інформаційні системи Київ: НАУ, 2007 152с.
- 3.2.8. Мокін Б.І., Мокін О.Б. Теорія автоматичного керування. Методологія та практика оптимізації /Навчальний посібник, Вінниця: ВНТУ, 2013, 210 с.

#### 3.3 Information resources on the Internet

- 3.3.1 http://www.infra.kth.se/~soh/decisiontheory
- 3.3.2 https://moluch.ru/archive/125/34485/
- 3.3.3 http://www.prorobot.ru/nauka/expert



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#### 4. RATING SYSTEM OF KNOWLEDGE AND SKILLS ASSESSMENT

4.1. Assessment of certain types of academic work performed by the student is carried out in points in accordance with table 4.1.

Table 4.1

Type of Academic Work	Maximum Grade Values	Type of Academic Work	Maximum Grade Values		
	Semeste	er №2			
Module №1 «Methodological four	ndations of	Module № 2 «Methods of dynamic o	ptimization		
optimal control systems	>	of control»			
Execution and defending laboratory works (total)	76×3 = 21	Execution and defending laboratory works (total)	76×3 = 21		
Execution of tasks of express control under time of laboratory classes	56×3 = 15	Execution of tasks of express control under time of laboratory classes	56×3 = 15		
For carrying out module test №1, a student must receive not less than	22	For carrying out module test №2, a student must receive not less than	22		
Module Test №1		Module Test №2	14		
<b>Total for the Module 1</b>	50	Total for the Module 2	50		
Total for modules 1, 2					
		Total for the subject	100		

*The credit rating* is determined (in points and on a national scale) based on the results of all types of educational work during the semester.

- 4.2. The kind of academic work, performed by a student, has been passed, if a student got positive grade.
- 4.3. The grades a student has been given for the different kinds of academic work the summed up and the result constituting a Current Module Grade is entered into the Module Grade Register.
- 4.4. In the case of **Graded test**, the sum of the final semester module grade in points constitutes the final semester rating grade, which is converted into a grade based on the national scale and the ECTS scale.
- 4.5. The Total Semester Grade is entered into the credit and examination information, the study card and into the student's record book, for example: 92/Ex/A, 87/Good/B, 79/Good/C, 68/Sat/D, 65/Sat./E, etc.
- 4.6. The Total Subject Grade corresponds to the Total Semester Grade. The Total Subject Grade is entered in the Diploma Supplement.



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 $(\Phi 03.02 - 01)$ 

# АРКУШ ПОШИРЕННЯ ДОКУМЕНТА

<b>№</b> прим.	Куди передано (підрозділ)	Дата видачі	П.І.Б. отримувача	Підпис отримувача	Примітки

 $(\Phi \ 03.02 - 02)$ 

АРКУШ ОЗНАЙОМЛЕННЯ З ДОКУМЕНТОМ

№ пор.	Прізвище, ім'я, по батькові	Підпис ознайомленої особи	Дата ознайом- лення	Примітки

 $(\Phi 03.02 - 04)$ 

# АРКУШ РЕЄСТРАЦІЇ РЕВІЗІЇ

<b>№</b> пор.	Прізвище, ім'я, по батькові	Дата ревізії	Підпис	Висновок щодо адекватності

 $(\Phi 03.02 - 03)$ 

### АРКУШ ОБЛІКУ ЗМІН

No		№ листа	(сторінки)	Підпис	Дата внесення зміни	Дата введення зміни	
зміни	Зміненого	Заміненого	го Нового Ану				особи, яка внесла зміну

 $(\Phi \ 03.02 - 32)$ 

### УЗГОДЖЕННЯ ЗМІН

	Підпис	Ініціали, прізвище	Посада	Дата
Розробник				
Узгоджено				
Узгоджено				
Узгоджено				